

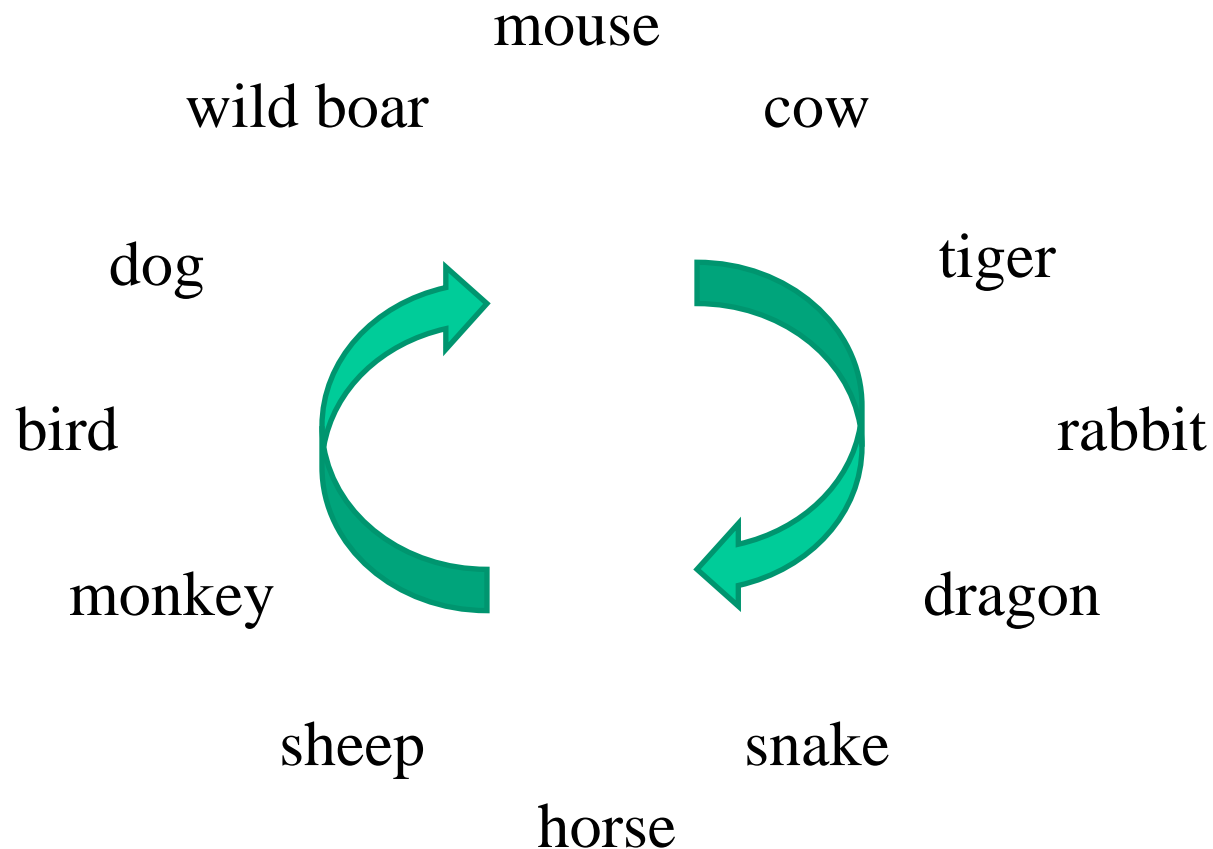
# Finding Preimages of Tiger Up To 23 Steps

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# Symbolic animal of the year



# Symbolic animal of the year



This year is a **TIGER** year !!

# Outline

□ Motivation

□ Tiger hash function

□ Pseudo-preimage attack on 23-step Tiger

□ Conclusion

# Recent progress in preimage attacks

- Since 2008, meet-in-the-middle preimage attacks have been developed for various MD4-based hash functions.
- Problems: weak message expansion  
(Reordering message index in each round)
- At CRYPTO'09, Aoki and Sasaki proposed an attack framework for linear message expansion.

*Is the attack applied to non-MD4-based hashes?*

# Design strategy of Tiger

	Tiger	MD4-family
Key schedule function	Non-linear expansion	Linear expansion
Non-linearity of step function	S-box	Bitwise Boolean function
Number of steps	24 (small)	At least 48 (large)
Word size	64 bits	32 bits
Shift/Rotation	Bit shift	Bit rotation

- Tiger's strategy:
  - strong and heavy computations
  - small number of rounds
- Can these prevent MitM preimage attacks?

# Comparison with previous work

## ◆ Preimage attack on Tiger (24steps for full specification)

	<i>#steps</i>	<i>complexity</i>	<i>memory</i>	<i>note</i>
Indestege <i>et al.</i>	13	$2^{128.5}$	<i>Negl.</i>	WeWoRC2007
Isobe <i>et al.</i>	16	$2^{161}$	$2^{32}$	FSE2009
Mendel	17	$2^{185}$	$2^{160}$	Africacrypt2009
<b>Ours</b>	<b>23</b>	<b><math>1.4 \times 2^{189}</math></b> <b><math>2^{187.5}</math></b>	<b><math>2^{22}</math></b> <b><math>2^{22}</math></b>	<b>Preimages</b> <b>2<sup>nd</sup> Preimages</b>
Guo <i>et al.</i>	24 (full)	$2^{184.3}$	$2^{16.7}$	ePrint 2010

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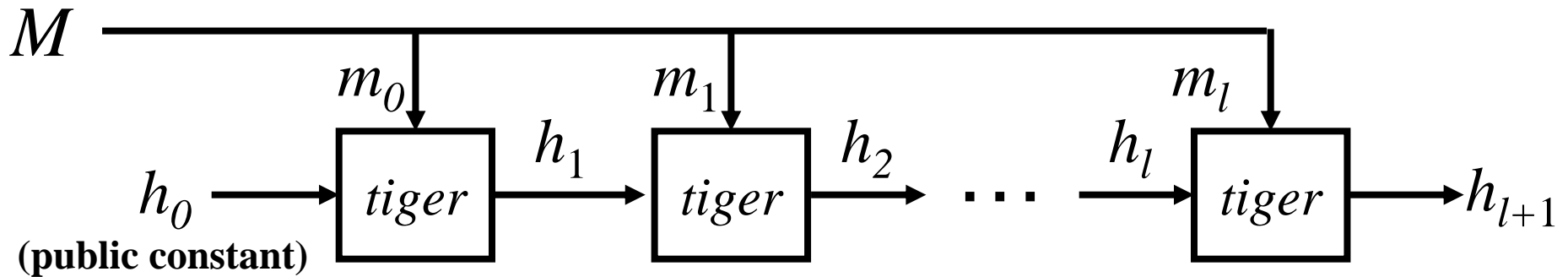
□ Conclusion



# Tiger

◆ An iterated hash function designed by Anderson and Biham.

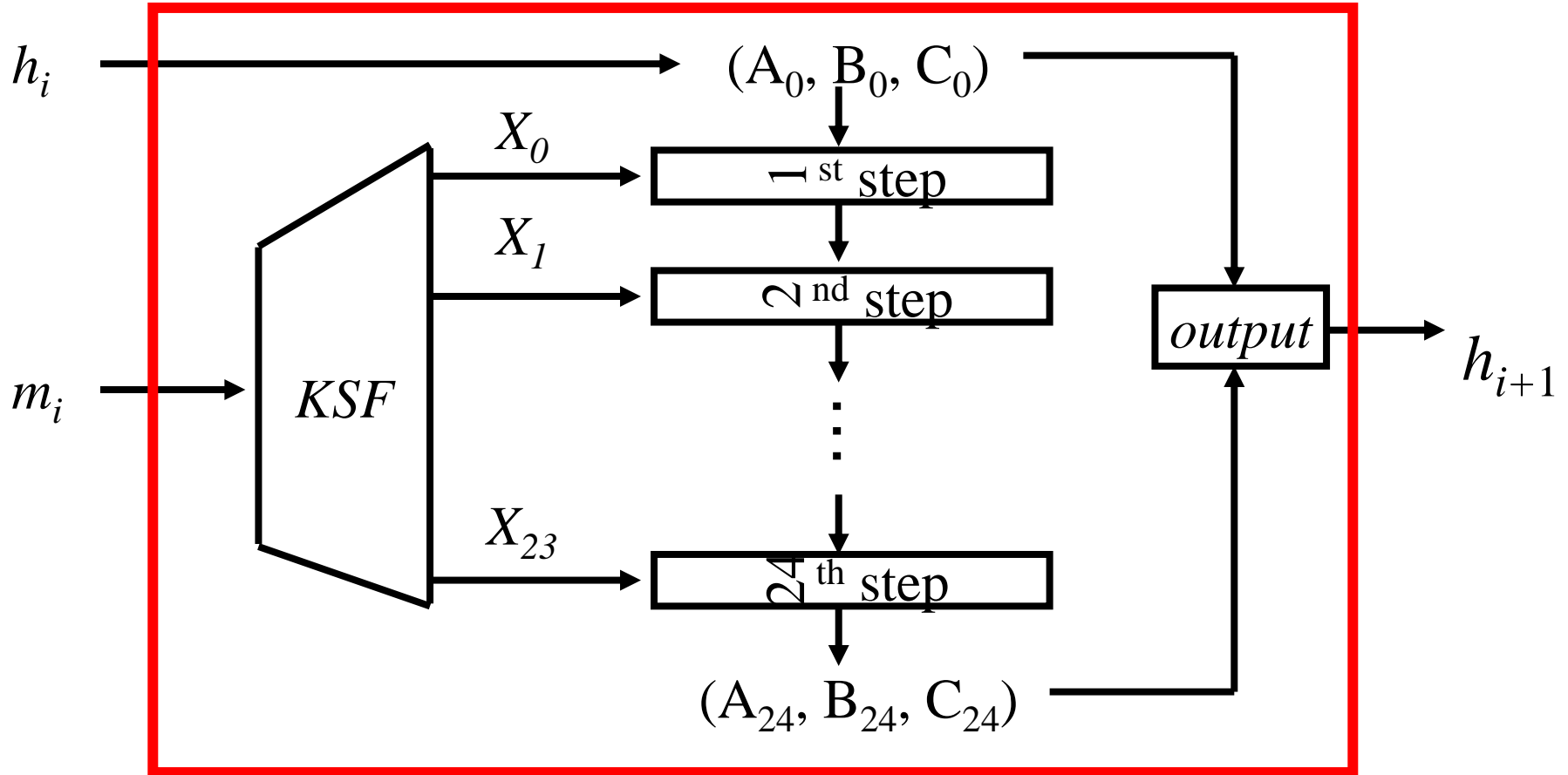
- Narrow-pipe Merkle-Damgård structure



- $m_i$ : 512 bits,  $h_i$ : 192 bits.
- $tiger$ : compression function of Tiger

$$\{0, 1\}^{192} \times \{0, 1\}^{512} \rightarrow \{0, 1\}^{192}$$

# Structure of *tiger*



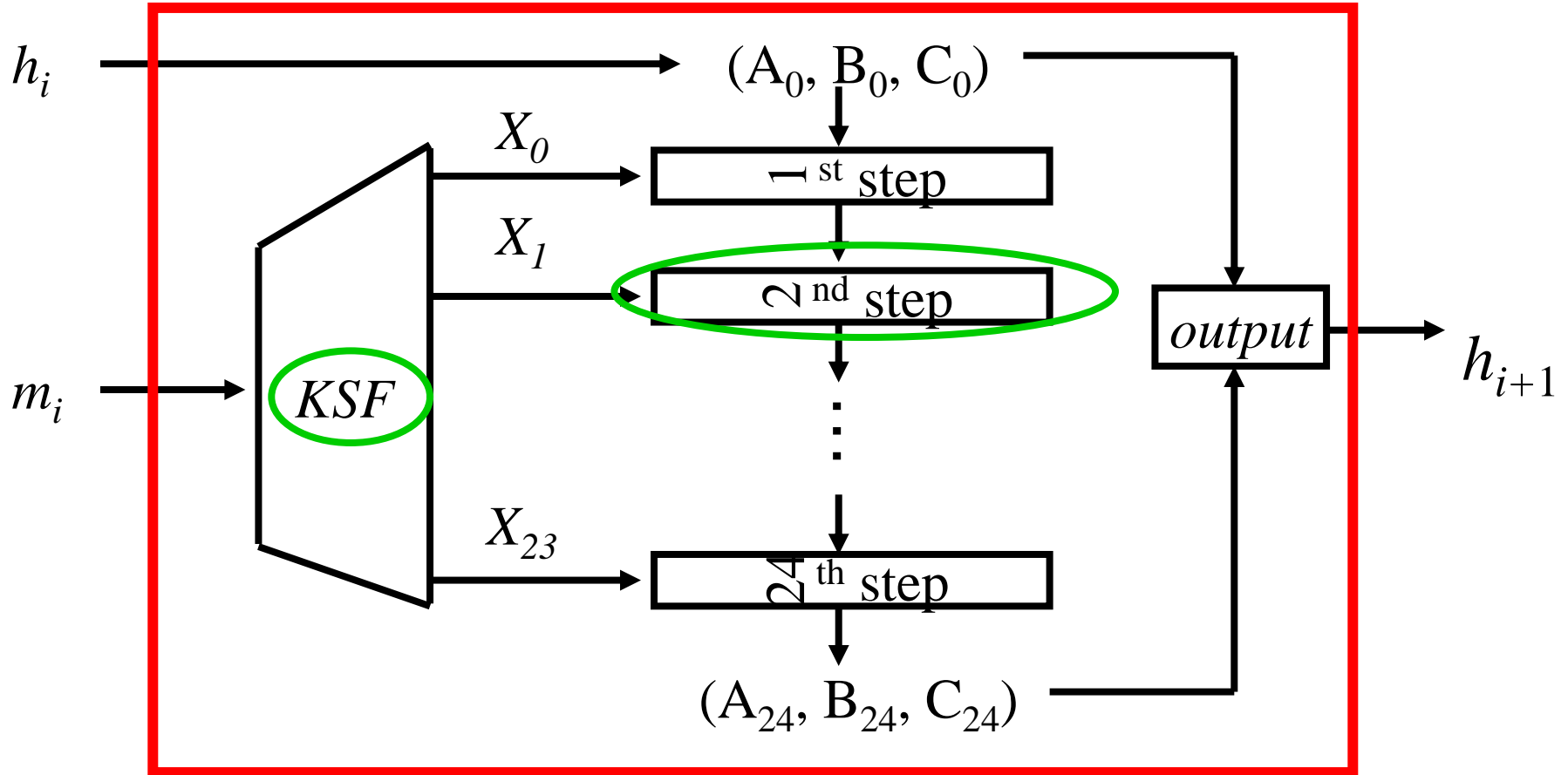
- $X_j, A_j, B_j, C_j$ : 64-bit

- $KSF$ : key schedule function

- $h_i = A_0 || B_0 || C_0$

- $h_{i+1} = (A_{24} \oplus A_0) || (B_{24} - B_0) || (C_{24} + C_0)$

# Structure of *tiger*



- $X_j, A_j, B_j, C_j$ : 64-bit

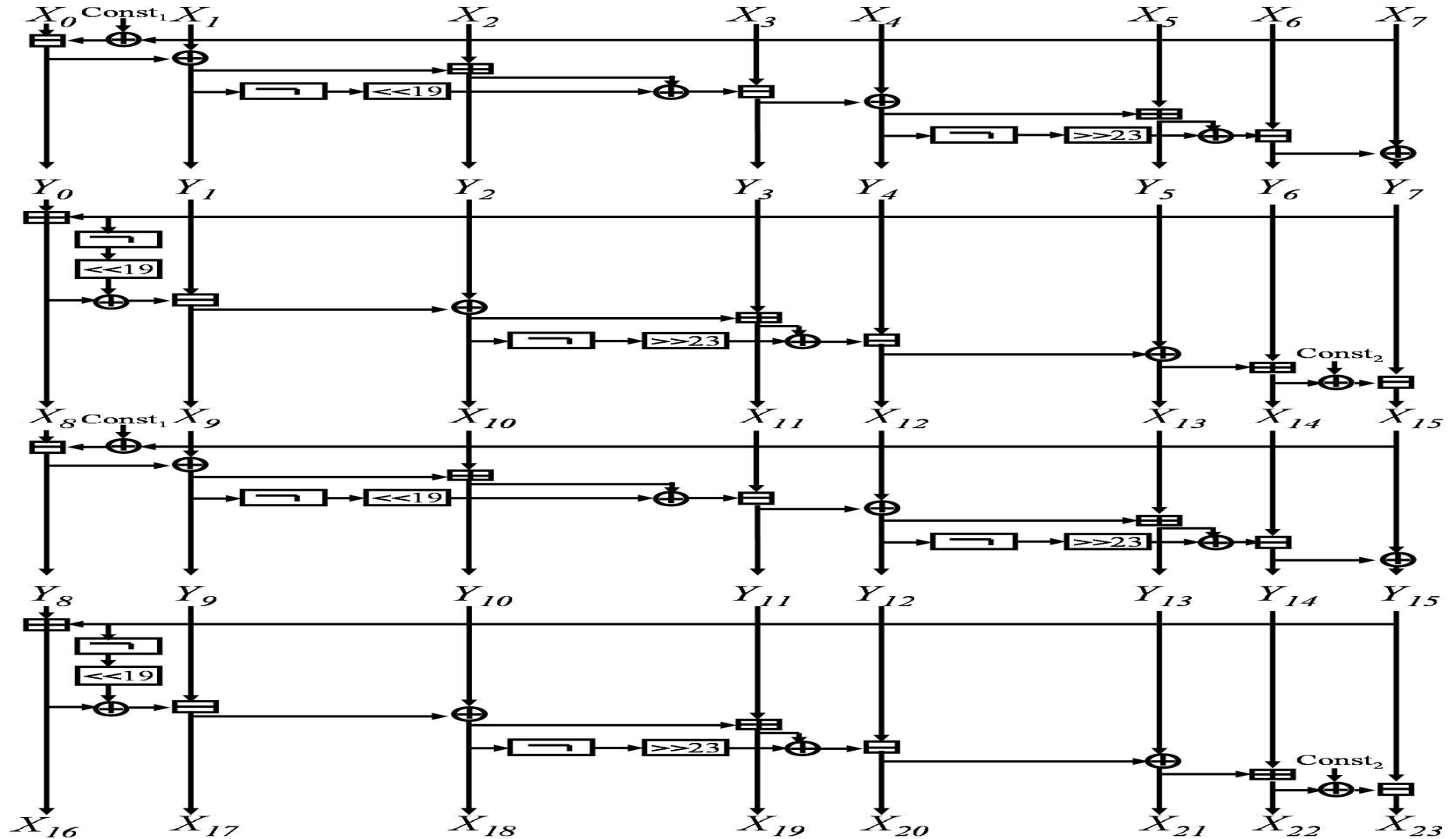
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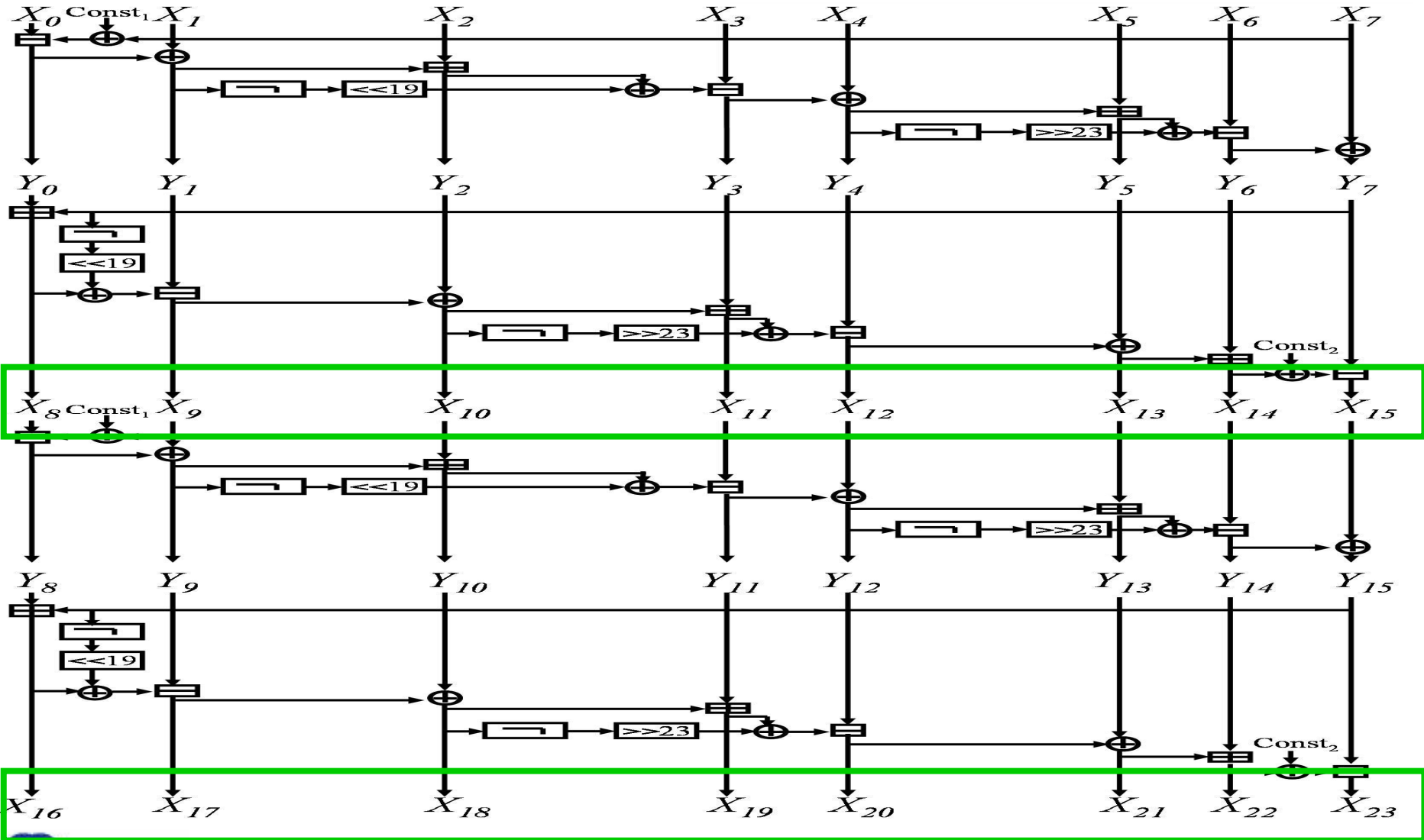
# KSF of tiger

◆  $m_i = X_0 // X_1 // X_2 // X_3 // X_4 // X_5 // X_6 // X_7$



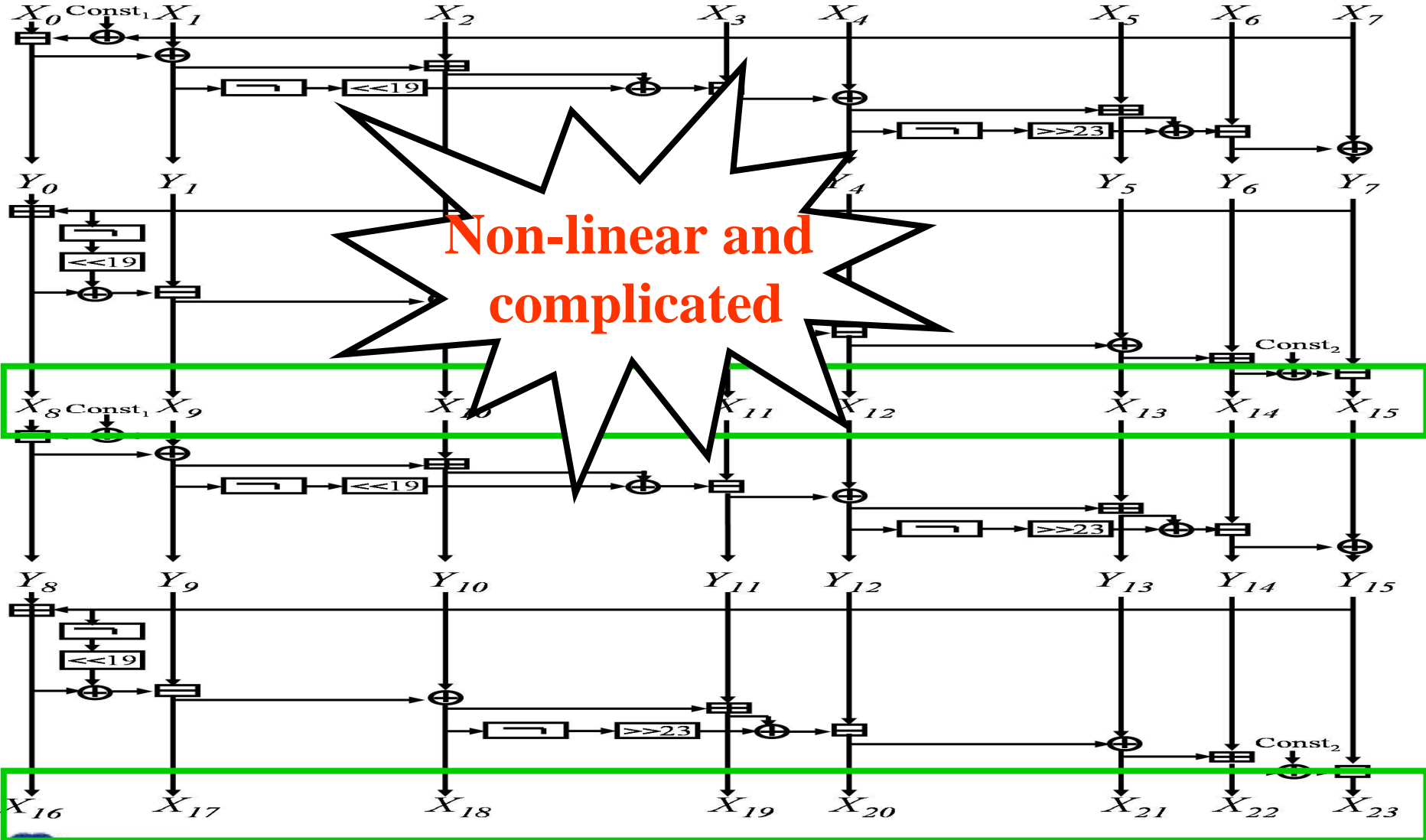
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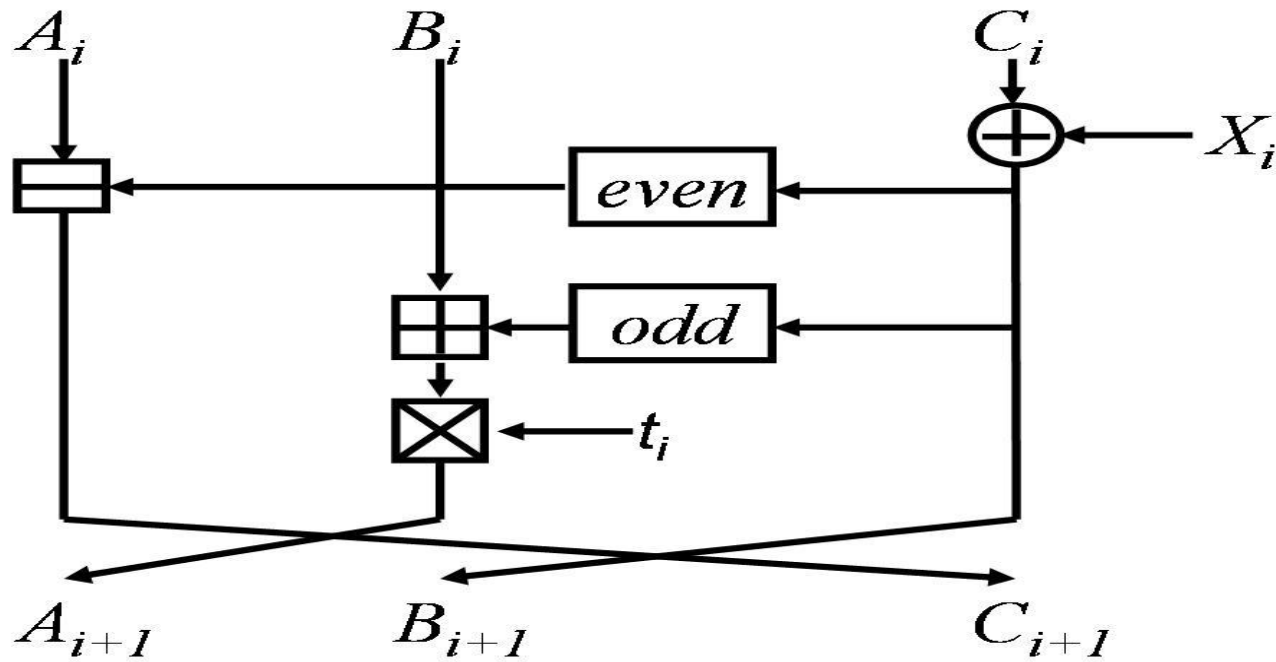


# KSF of tiger

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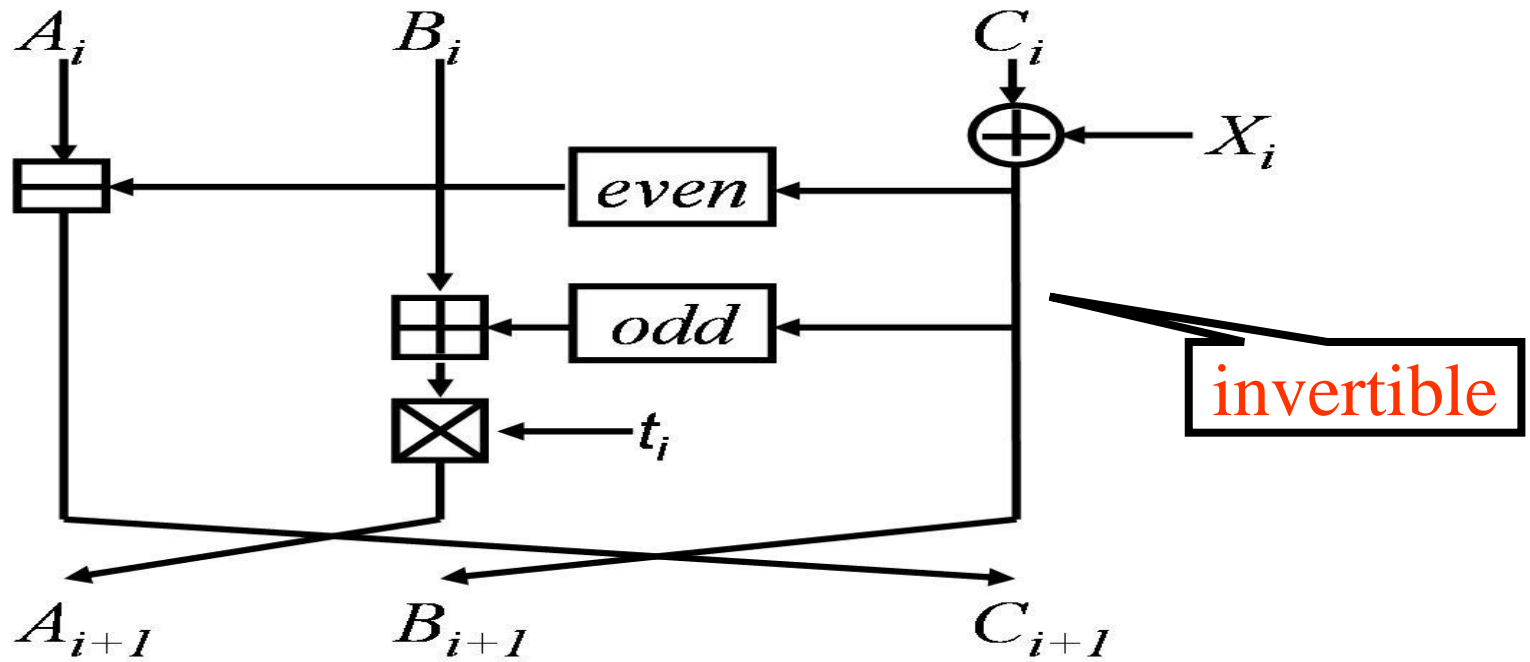


# Step function of *tiger*



- $X_i \oplus C_i = c_7 // c_6 // \dots // c_0$
- $c_j$ : 8-bit
- $t_i$ : a small constant
- $even = T_0(c_0) \oplus T_1(c_2) \oplus T_2(c_4) \oplus T_3(c_6)$
- $odd = T_3(c_1) \oplus T_2(c_3) \oplus T_1(c_5) \oplus T_0(c_7)$
- $T_j$ : S-boxes mapping 8-bit values to 64-bit values

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# Outline

□ Motivation

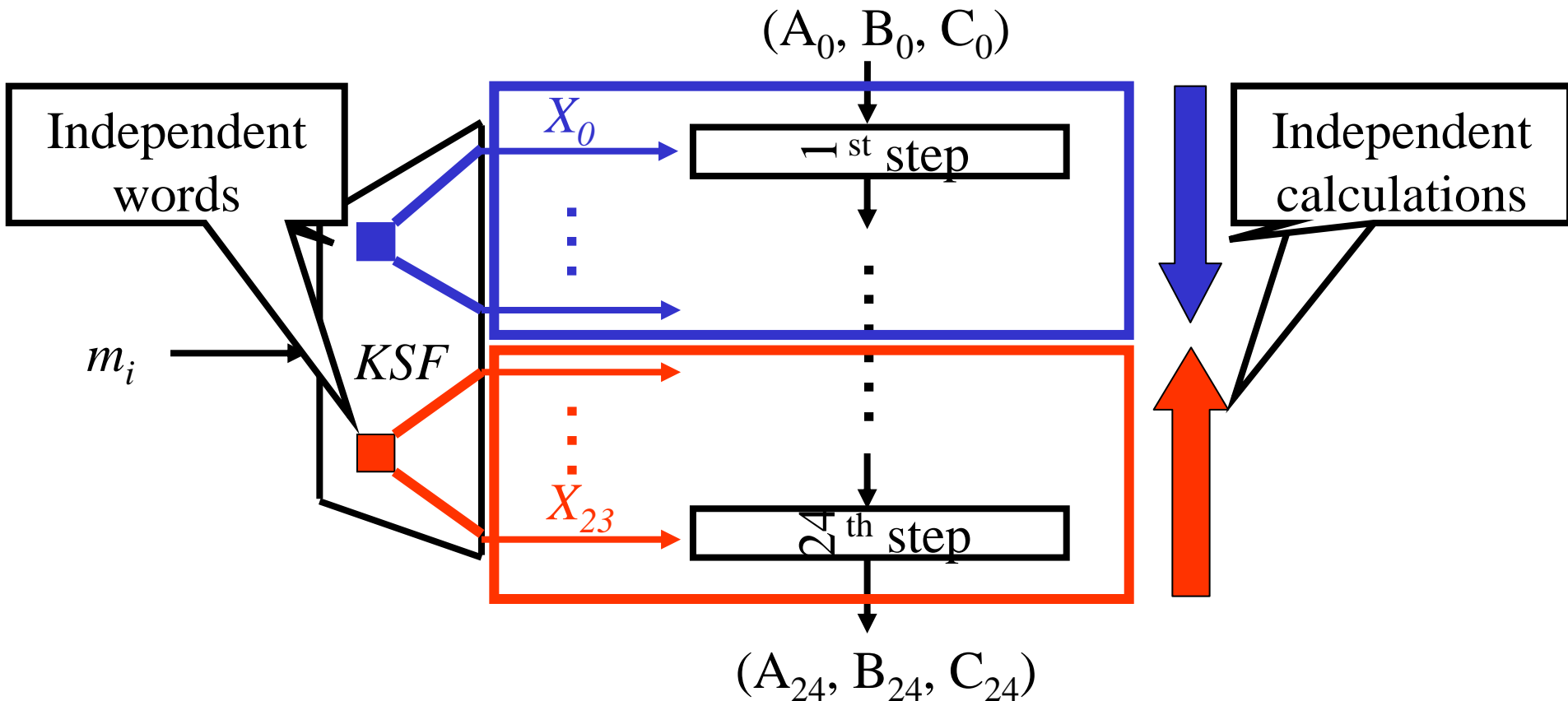
□ Tiger hash function

□ Pseudo-preimage attack on 23-step Tiger

□ Conclusion

# Attack scenario

- ◆ Meet-in-the-middle approach: based on weakness of *KSF*.



- ◆ Finding pseudo-preimages is enough for finding preimages.

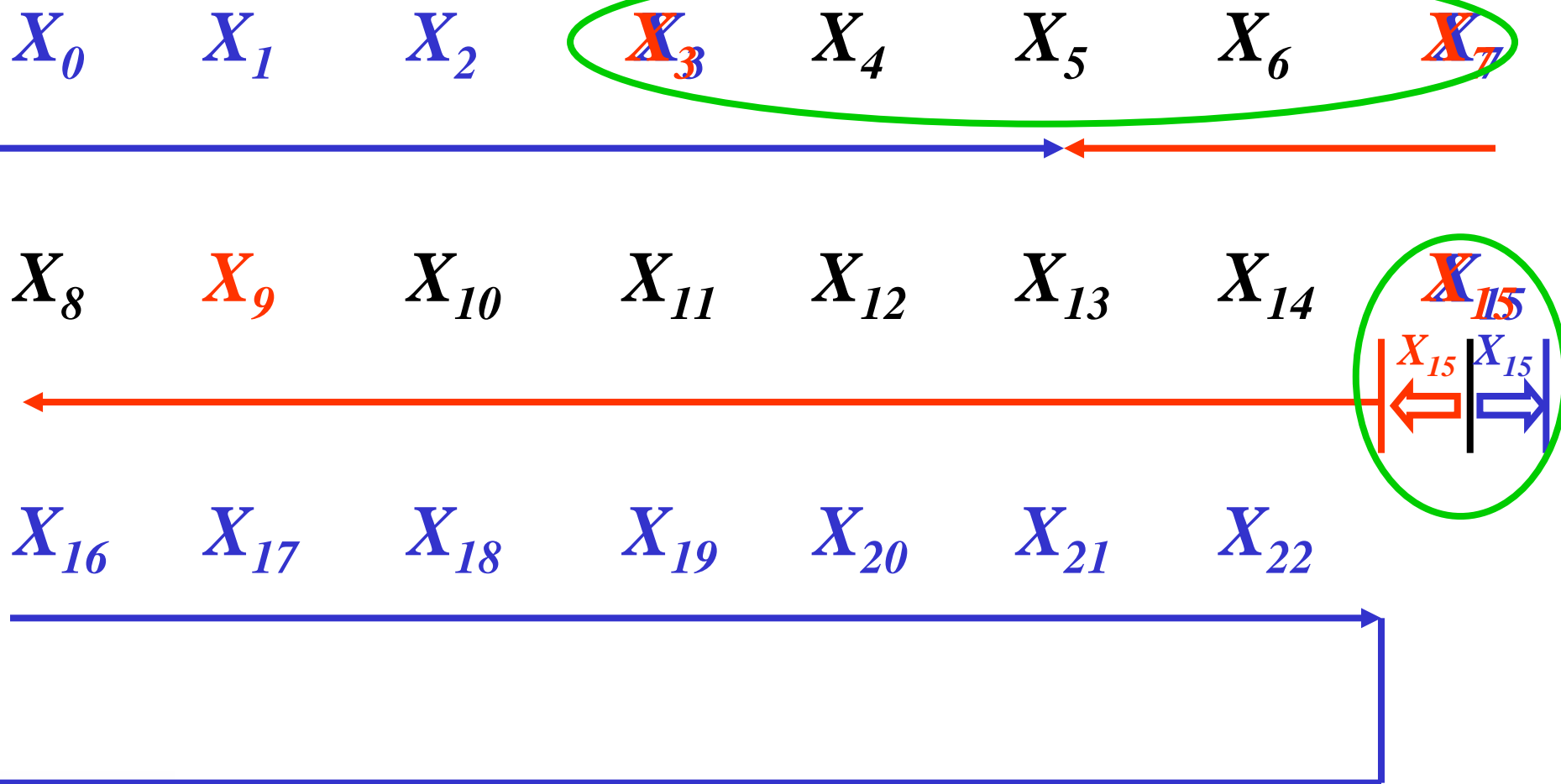
# Our independent words: ( $X_{15}$ , $X_{23}$ )

◆  $X_{15}$  changes its 11 LSBs\*, and  $X_{23}$  changes its 19 MSBs.

$X_0$	$X_1$	$X_2$	<del><math>X_3</math></del>	$X_4$	$X_5$	$X_6$	<del><math>X_7</math></del>
$X_8$	<del><math>X_9</math></del>	$X_{10}$	$X_{11}$	$X_{12}$	$X_{13}$	$X_{14}$	<del><math>X_{15}</math></del>
$X_{16}$	$X_{17}$	$X_{18}$	$X_{19}$	$X_{20}$	$X_{21}$	$X_{22}$	<del><math>X_{23}</math></del>

# Overview of our attack

◆ We use message words to represent the corresponding step function.



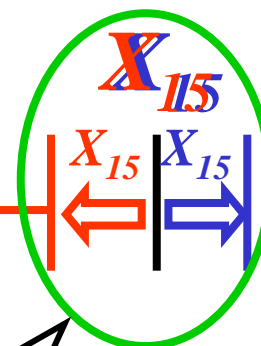
# Overview of our attack

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$X_0$     $X_1$     $X_2$     ~~$X_3$~~     $X_4$     $X_5$     $X_6$     ~~$X_7$~~

$X_8$     ~~$X_9$~~     $X_{10}$     $X_{11}$     $X_{12}$     $X_{13}$     $X_{14}$

$X_{16}$     $X_{17}$     $X_{18}$     $X_{19}$     $X_{20}$     $X_{21}$     $X_{22}$

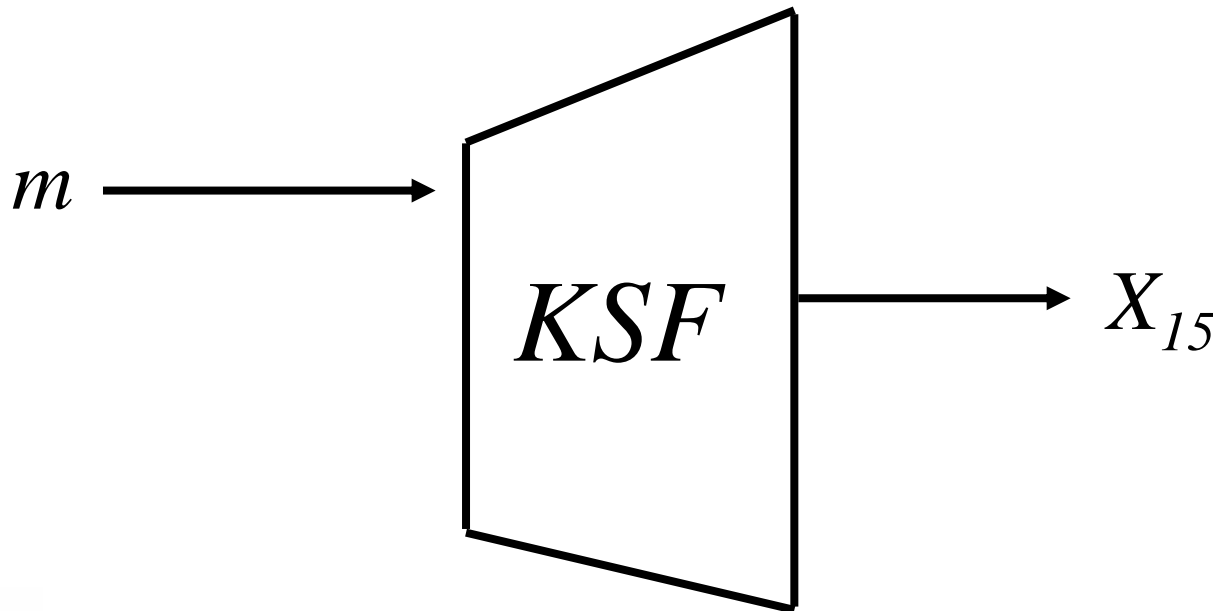


Initial-structure

Split  $X_{15}$  into independent  $X_{15}^u$  and  $X_{15}^l$

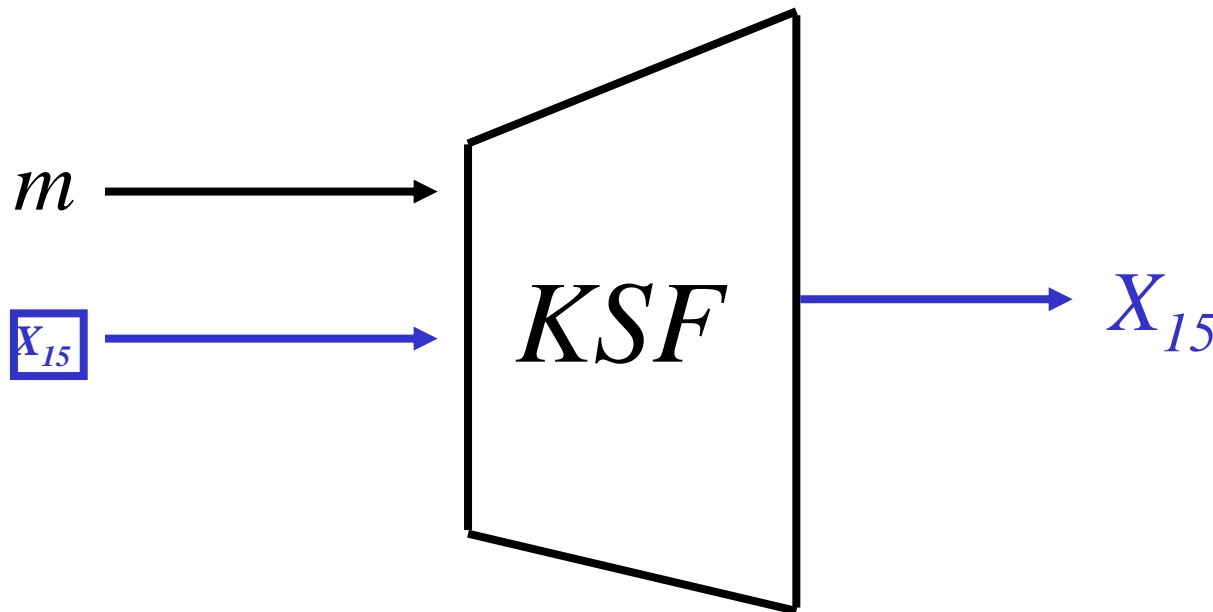
◆ Split  $X_{15}$  into upper and lower halves

Original  $X_{15}$



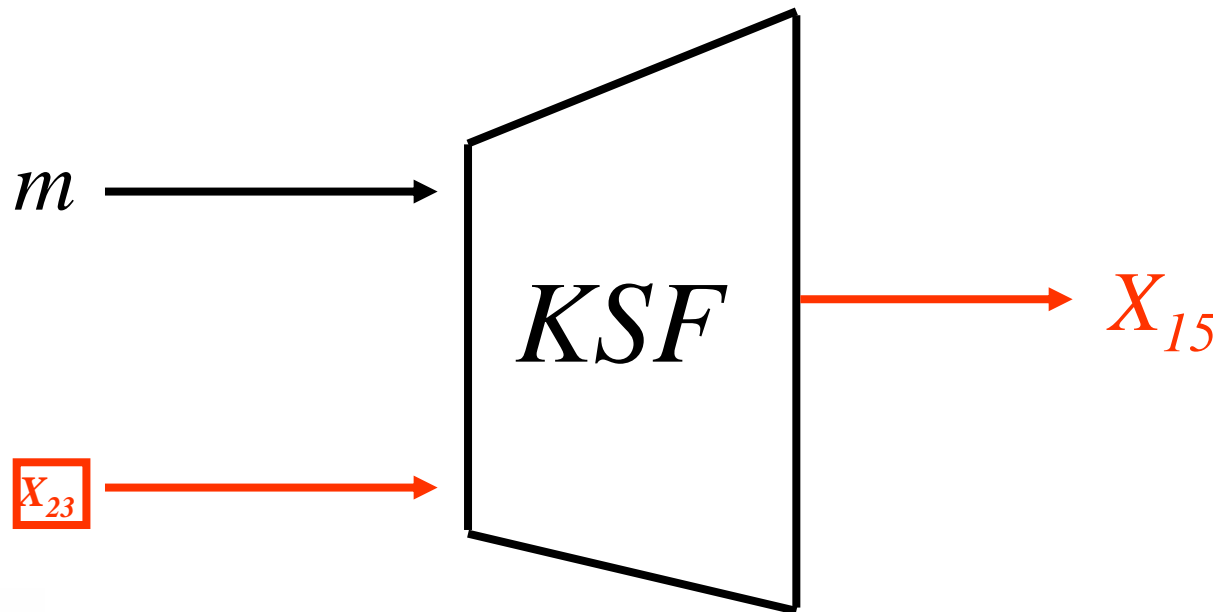
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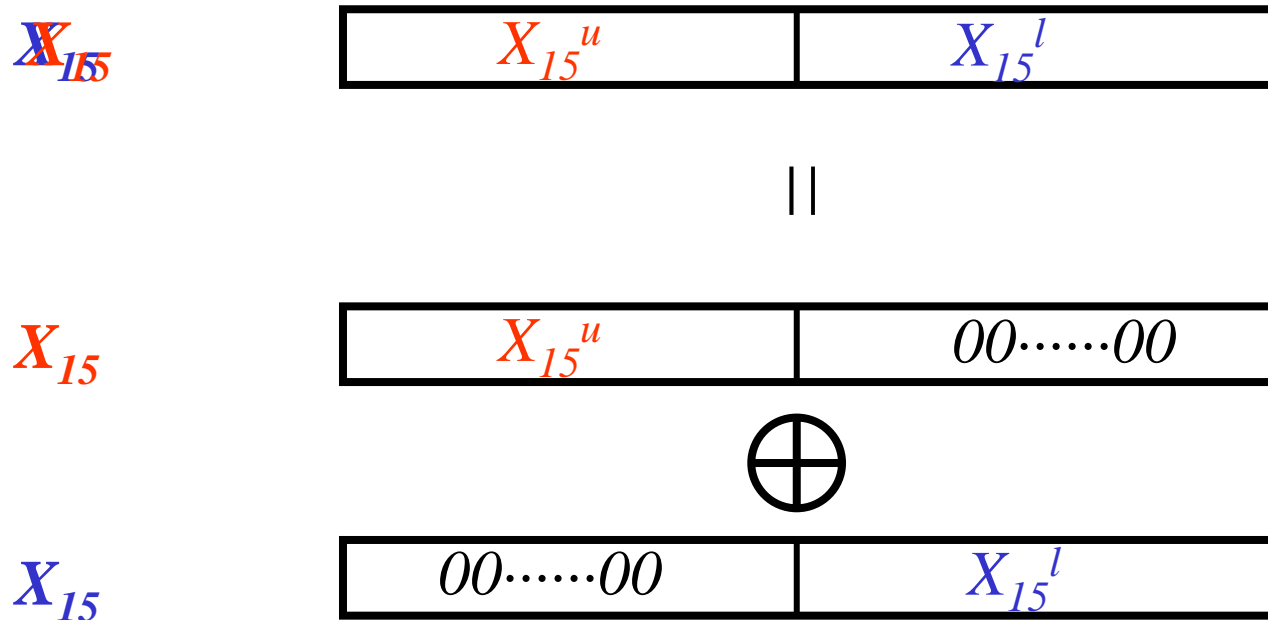
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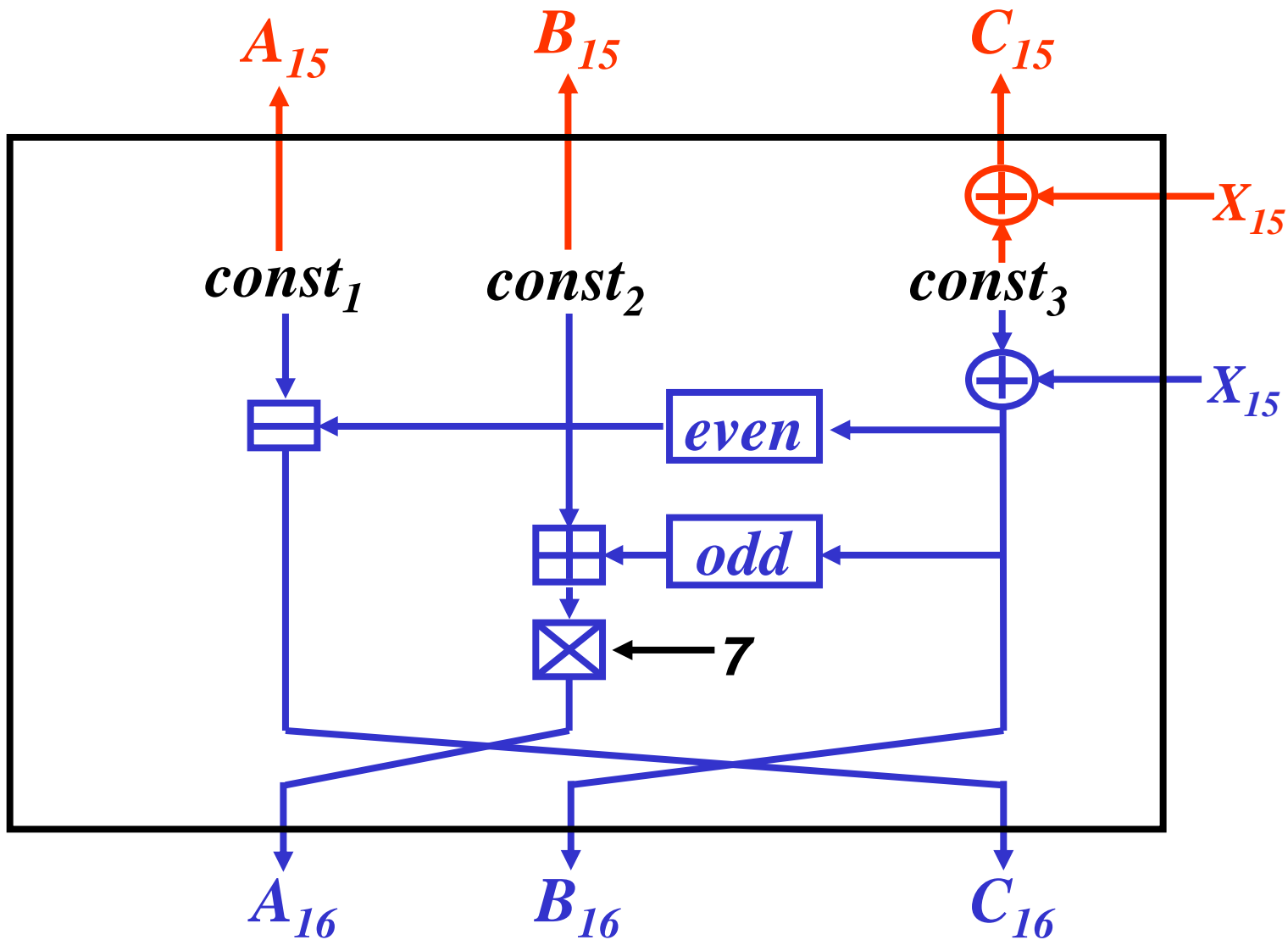


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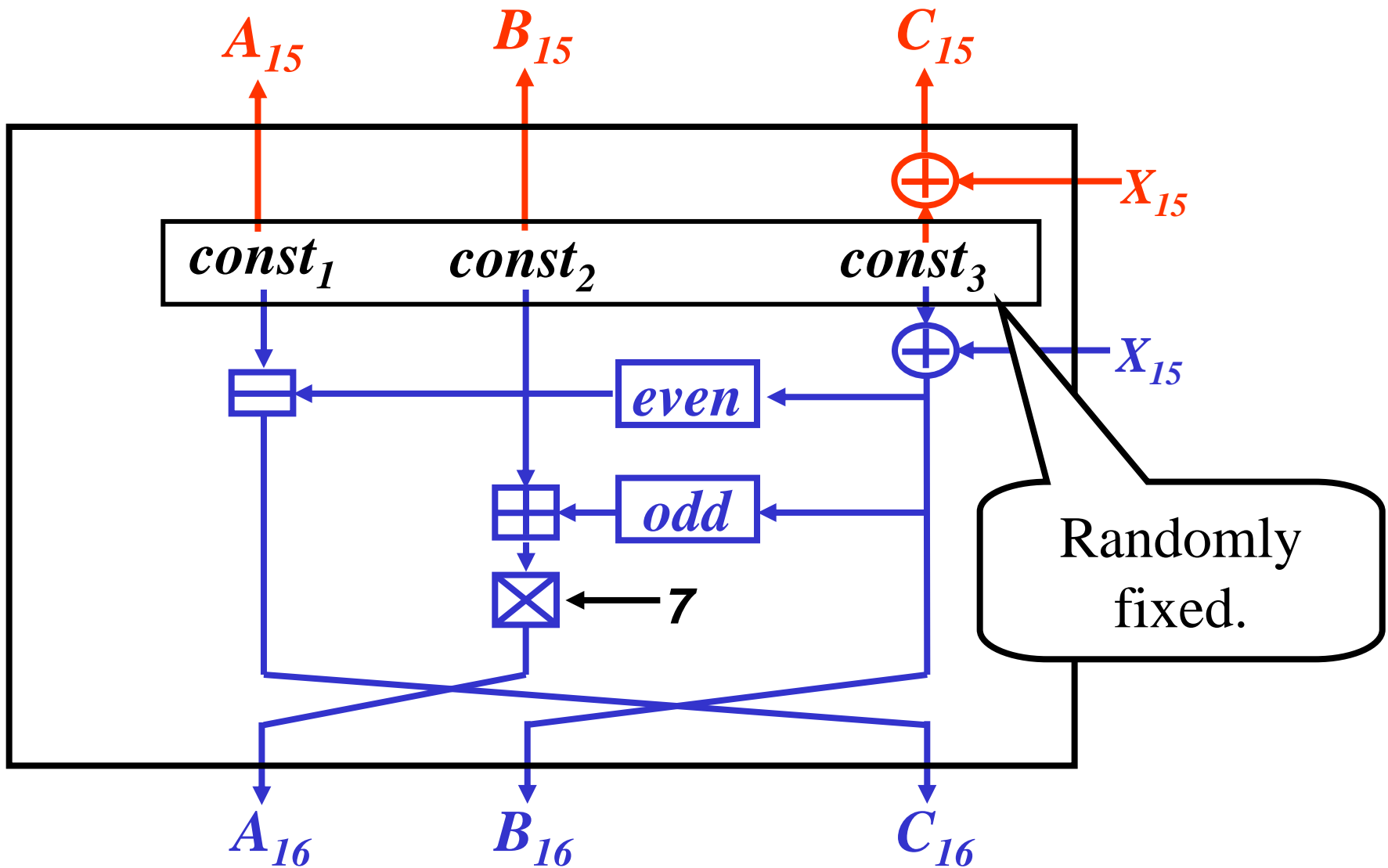
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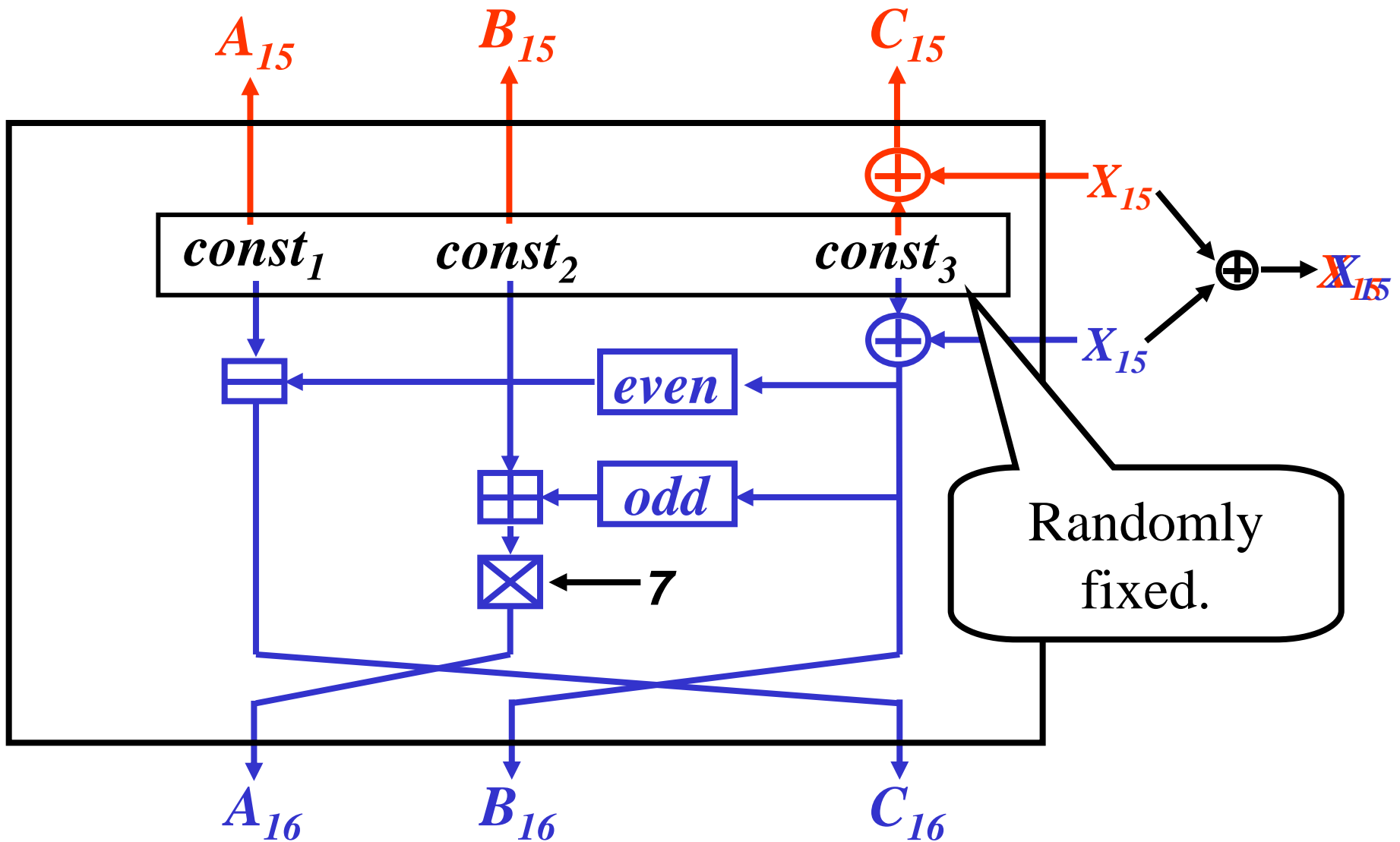
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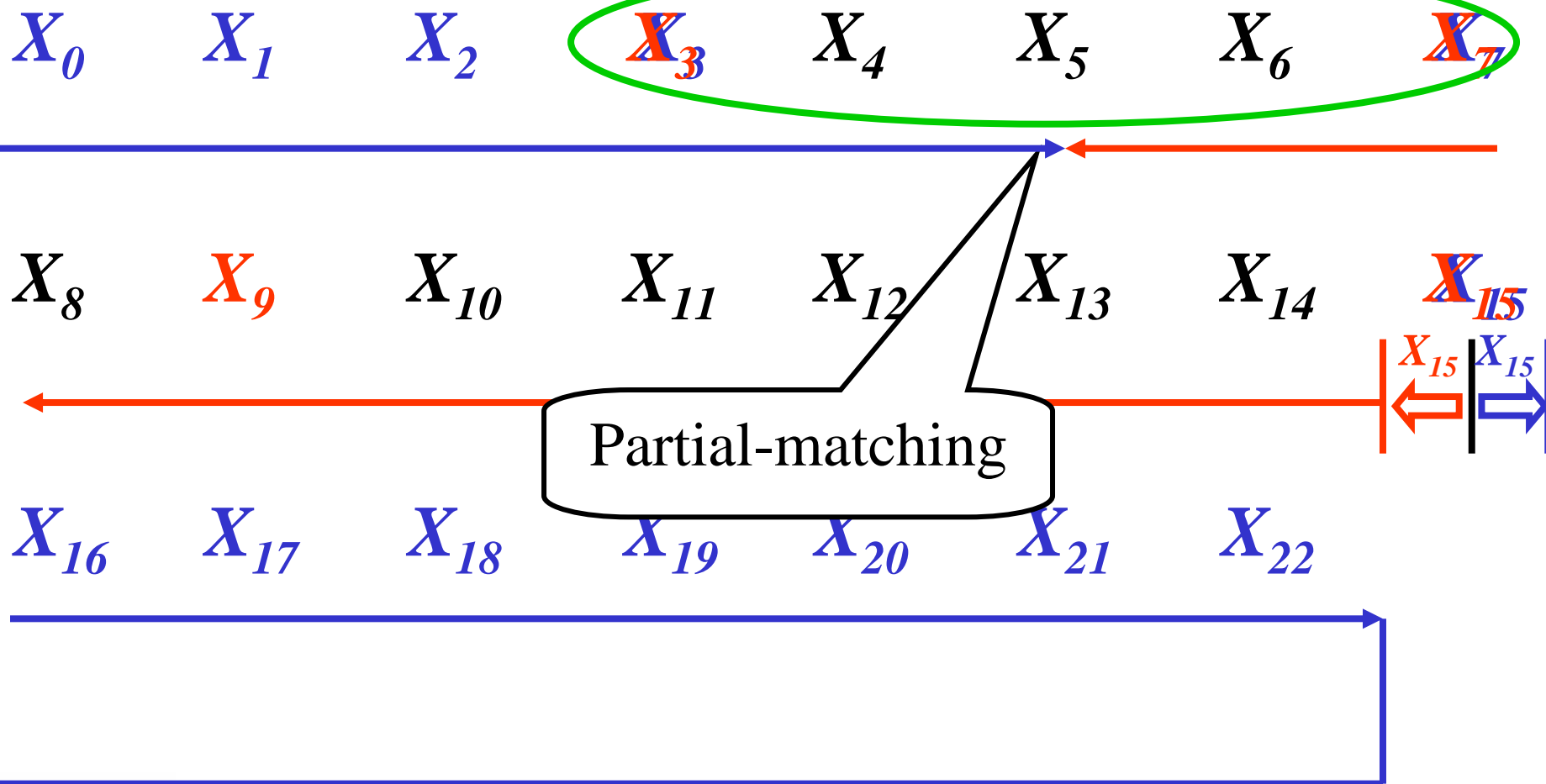


# Initial structure at step 16



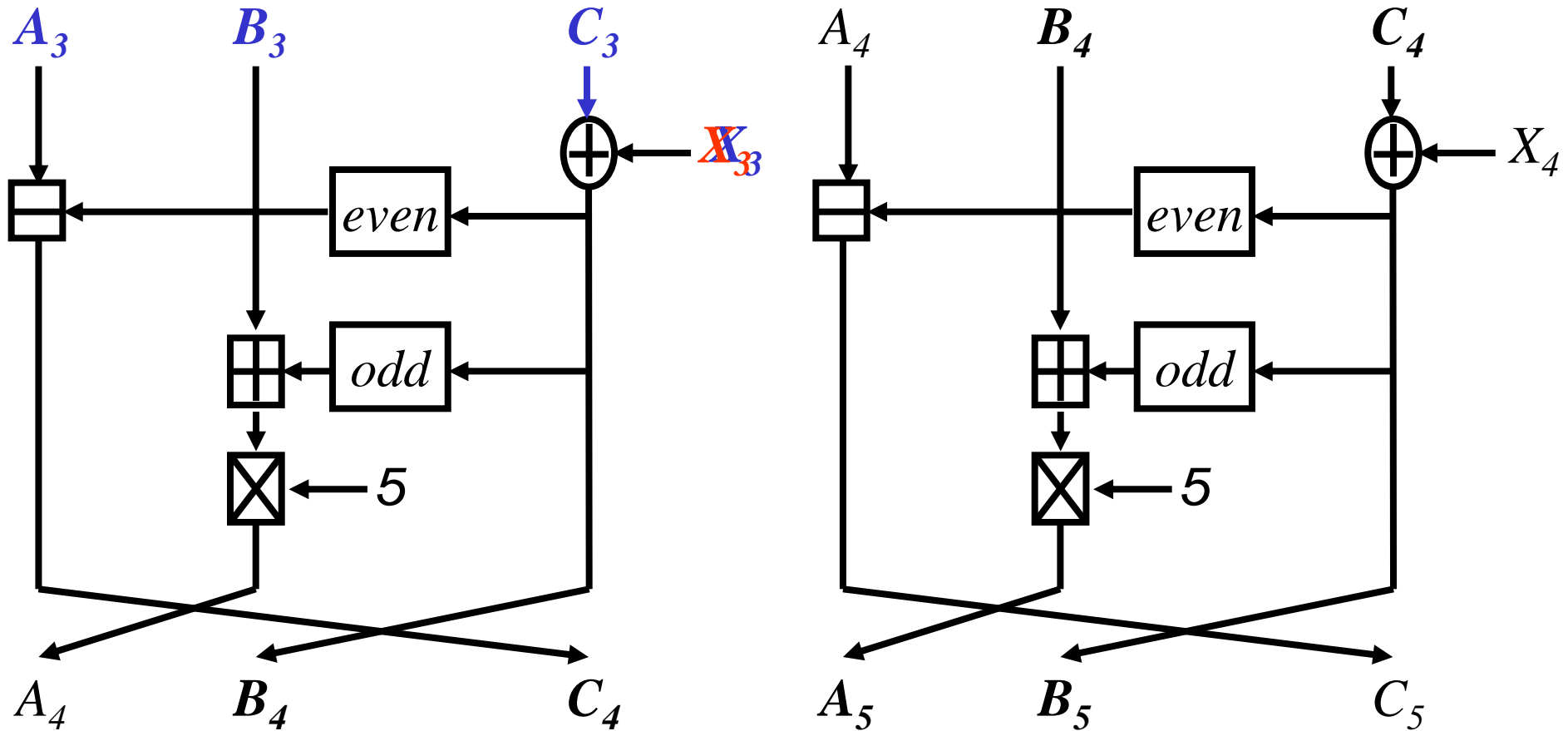
# Overview of our attack

- ◆ We use message words to represent the corresponding step function.



# Calculation from step 4 to 5

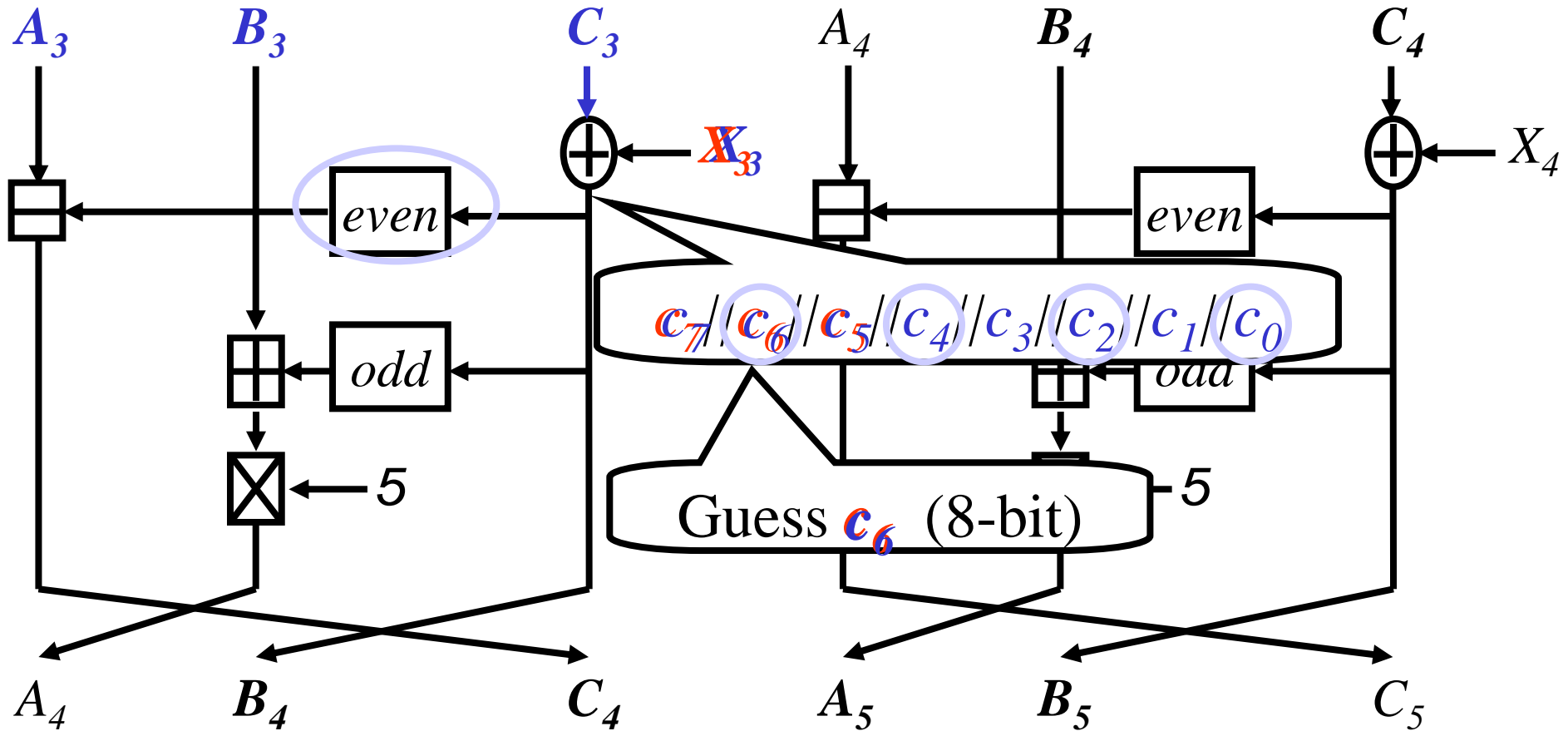
◆ Note that **red** word only change 19 MSBs of  $X_3$ .





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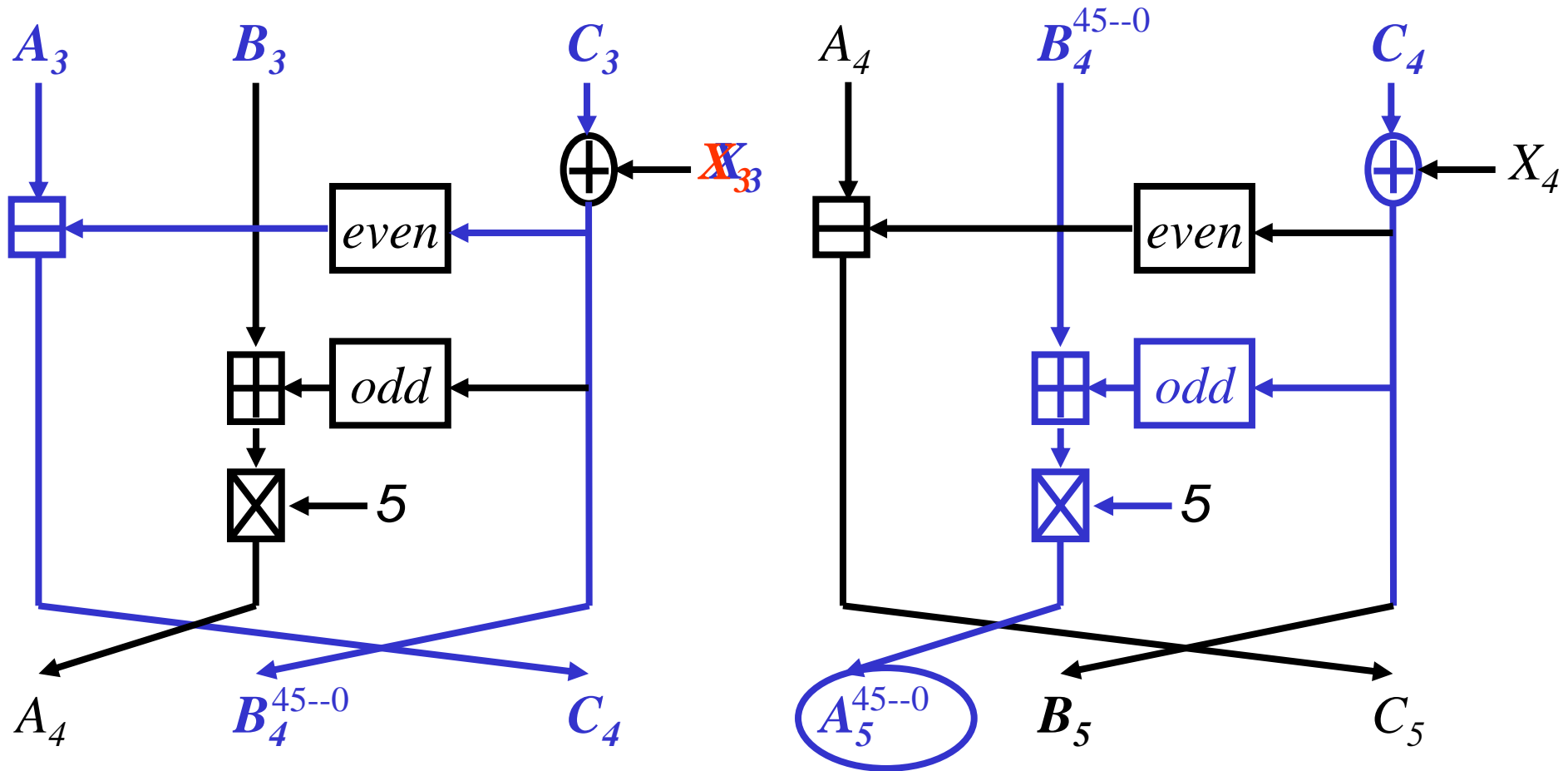
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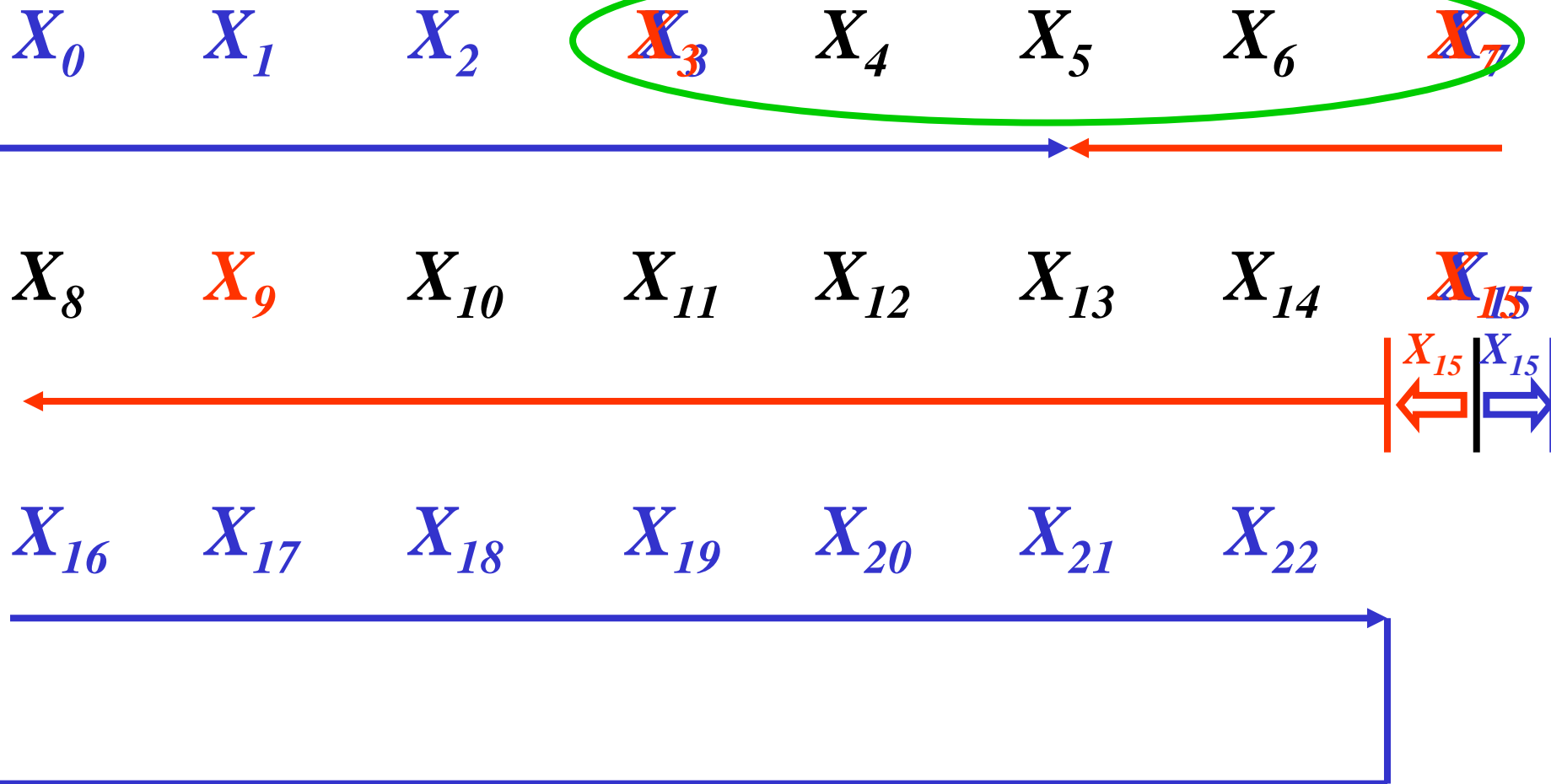


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# Overview of our attack





# Evaluating the complexity

- ◆ Recall that  $X_{15}$  changes its 11 LSBs and  $X_{23}$  changes its 19 MSBs.

#elements:  $2^{11}$

$\mathcal{T}$   
 $(\dots, A_3, B_3, C_3)^1$   
 $(\dots, A_3, B_3, C_3)^2$   
⋮

Exhaustively  
guess 8 bits

#elements:  $2^{19}$

$\mathcal{T}$   
 $(\dots, A_5^{1,45--0})$   
 $(\dots, A_5^{2,45--0})$   
⋮

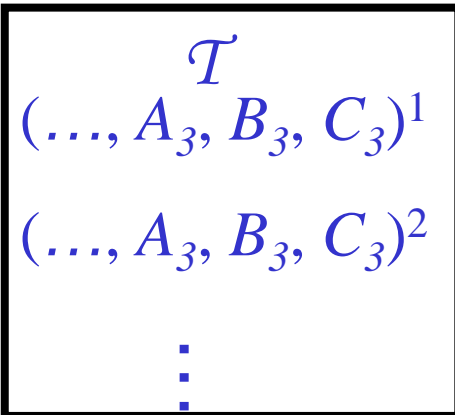
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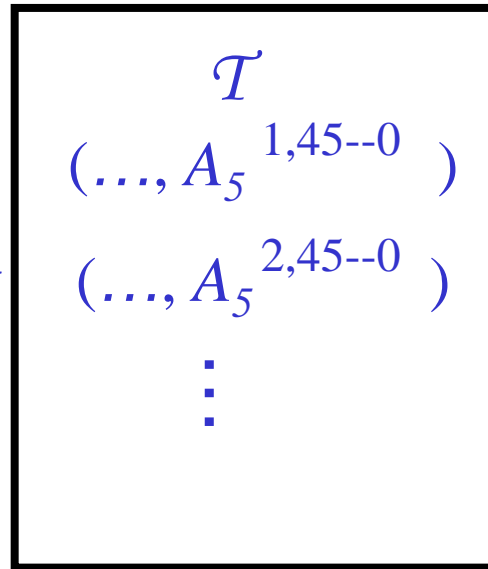
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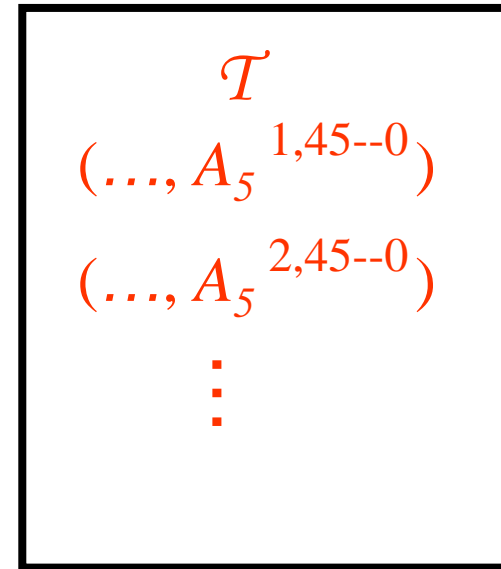


Exhaustively  
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- ◆  $2^{19}$  tiger computations will contribute to  $2^{38}$  pairs.

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- ◆  $2^{19}$  tiger computations will contribute to  $2^{38}$  pairs.
- ◆ For each pair, the success probability of guess is  $2^{-8}$ .

# Evaluating the complexity

- ◆ Recall that  $X_{15}$  changes its 11 LSBs and  $X_{23}$  changes its 19 MSBs.

#elements:  $2^{11}$

$\mathcal{T}$   
 $(\dots, A_3, B_3, C_3)^1$

#elements:  $2^{19}$

$\mathcal{T}$   
 $(\dots, A_5^{1,45--0})$

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$\mathcal{T}$   
 $(\dots, A_5^{1,45--0})$

Finally the complexity of finding a pseudo-preimage is  $2^{181}$  ( $2^{192-19+8}$ ).

- ◆  $2^{19}$  tiger computations will contribute to  $2^{38}$  pairs.
- ◆ For each pair, the success probability of guess is  $2^{-8}$ .

# Note on preimage attacks

- We use the generic conversion from pseudo-preimages to preimages.  
→ (2<sup>nd</sup>) preimages with a complexity of  $2^{187.5}$ .
- If padding is considered, message freedom in an independent chunk is reduced by 9 bits.  
→ preimages with a complexity of  $1.4 \times 2^{189}$ .



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# Conclusion

- ◆ We have found a preimage attack on **23-step Tiger** based on the recently developed MitM approach.
- ◆ The complexity of our attack is as follows:

	<b>Time</b>	<b>Memory</b>
<b>Preimages</b>	$1.4 \times 2^{189}$	$2^{22}$
<b>2<sup>nd</sup> Preimages</b>	$2^{187.5}$	$2^{22}$

*Thank you for your attention !!*